## Dynamics of the Sea Breeze in the Atmospheric Boundary Layer: A Case Study of the Free Convection Regime

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ABSTRACT—Simultaneous measurements of temperature and wind profiles in the surface boundary layer (below 10-m elevation over a beach and below 100-m elevation over an inland site) under the effect of the sea breeze were made near Fort Walton Beach, Fla. We found that the sea breeze in the atmospheric boundary layer is in the free

convection regime and that observed sea-breeze wind and temperature profiles behave according to minus one-third power laws. These experiments also substantiate evidence that the Prandtl-Obukhov-Priestley prediction of the free convection regime is a valid one under appropriate atmospheric conditions.

### 1. INTRODUCTION

Prandtl (1932), Obukhov (1971), and Priestley (1954) have pointed out independently that the asymptotic state of turbulence in an unstable stratified boundary layer (e.g., the free convection regime in the atmosphere) requires that

 $\frac{\partial \theta}{\partial z} \sim z^{-4/3}$   $\frac{\partial U}{\partial z} \sim z^{-4/3}$ (1)

and

where  $\theta$  is the potential temperature, z is the height coordinate, and U is the magnitude of the horizontal wind.

According to Businger and Yaglom (1971), observations of truly free convection conditions are still scarce, and experimental confirmation of the Prandtl-Obukhov-Priestley predictions has been, until now, somewhat in doubt (Dyer 1965, Elliott 1966, Businger et al. 1971). Businger and Yaglom suggested that a careful study of the free convection case in the atmosphere is still needed. In partial response to this suggestion, a case study of the free convection regime in the atmospheric boundary layer that exists under the sea-breeze condition is given in this paper. Particular emphasis, however, is on the sea-breeze wind profile inasmuch as the temperature fluctuations associated with the free convection regime have been verified by Wyngaard et al. (1971). Some evidence of sea breeze associated with the free convection regime has been given elsewhere (Hsu 1970a).

### 2. THEORETICAL CONSIDERATIONS

The following derivation for the sea-breeze regime in the surface boundary layer is due in part to McPherson (1970) and is an expanded version of that presented by Estoque (1961).

It is presumed that, in the layer immediately above the surface, the viscous forces acting on a fluid element are much larger than the inertial forces; thus, the horizontal momentum equations and the thermodynamic equation for the layer become

$$\frac{\partial}{\partial z} \left( K \frac{\partial U}{\partial z} \right) = 0 \tag{2}$$

and

$$\frac{\partial}{\partial z} \left( K \frac{\partial \theta}{\partial z} \right) = 0 \tag{3}$$

where K is an eddy exchange coefficient, assumed to be the same for both heat and momentum transfer, U is the magnitude of the horizontal wind, and  $\theta$  is the potential temperature. If K is known as a function of height, z, the equations can be integrated to obtain U and  $\theta$  in the boundary layer.

Under conditions of free convection; that is, when the buoyant forces dominate the mechanical forces, the expression of K is, as discussed by Priestley (1959),

$$K = \lambda z^2 \left( \frac{g}{\theta} \left| \frac{\partial \theta}{\partial z} \right| \right)^{1/2}$$
 Ri<-0.03. (4)

Here,  $\lambda$  is an empirical constant, g is the acceleration due to gravity, and  $\overline{\theta}$  is a layer-mean potential temperature in the layer in which the Richardson number, Ri, is evaluated. Equations (2) and (3) may be written as

$$K\frac{\partial U}{\partial z} = U_*^2 \tag{5}$$

and

$$K\frac{\partial \theta}{\partial z} = \theta_* U_* \tag{6}$$

where  $U_*$  and  $\theta_*$  are termed the "friction velocity" and "friction temperature," respectively. From eq (5) and (6),



FIGURE 1.—Cup anemometer array located in the midforeshore on the coast of the Gulf of Mexico near Fort Walton Beach. A hotwire anemometer array on the taller offshore mast and a resistancewire wave gage and an air-sea temperature recording unit on the shorter mast are shown in the background.

we obtain

$$\frac{\partial U}{\partial z} = \frac{U_*}{\theta_*} \frac{\partial \theta}{\partial z} \tag{7}$$

and

$$\frac{\partial \theta}{\partial z} = \frac{\theta_*}{U_*} \frac{\partial U}{\partial z}.$$
 (8)

For the free convection regime, we use eq (4)-(8) and obtain

$$\frac{\partial U}{\partial z} = \left(\frac{U_{\bullet}^{5}\overline{\theta}}{\lambda^{2}g|\theta_{\bullet}|}\right)^{1/3}z^{-4/3} \tag{9}$$

and

$$\frac{\partial \theta}{\partial z} = \left(\frac{U_*^2 \theta_*^2 \overline{\theta}}{\lambda^2 g}\right)^{1/3} z^{-4/3} \tag{10}$$

Equations (9) and (10) can be integrated between two arbitrary levels,  $z_1$  and  $z_2$ , to give

$$U(z_1) - U(z_2) = -3 \left( \frac{U_*^5 \vec{\theta}}{\lambda^2 g |\theta_*|} \right)^{1/3} (z_1^{-1/3} - z_2^{-1/3})$$
 (11)

and

$$\theta(z_1) - \theta(z_2) = -3 \left( \frac{U_{*}^2 \theta_{*}^2 \overline{\theta}}{\lambda^2 g} \right)^{1/3} (z_1^{-1/3} - z_2^{-1/3}). \tag{12}$$

Equation (11) can be rewritten as

$$U=3\left(\frac{U_{*}^{5}\overline{\theta}}{\lambda^{2}g|\theta_{*}|}\right)^{1/3}(z_{0}^{-1/2}-z^{-1/3})$$
 (13)

in which  $z_0$  is the roughness length [i.e., from eq (11),  $U(z_1)=0$  at  $z_1=z_0$ ]. Note that the wind profile [eq (13)] involves no logarithmic height dependency; that is, in the atmospheric free convection regime, the familiar logarithmic wind profile (e.g., Haltiner and Martin 1957) is no longer a valid one.

### 3. FIELD EXPERIMENTS

## Field Sites and Experiments

Two experimental sites, located on the gulf coast near Fort Walton Beach, Fla., were selected. One was the beach site shown in figure 1 (86°43′W, 30°24′N), which has an approximate east-west shoreline orientation. It was used in an earlier study of the local wind system (Hsu 1969). The experiment discussed in this study was performed during May 1970. It was designed to measure the wind and temperature profiles in the surface boundary layer, as shown in eq (11) and (12), respectively.

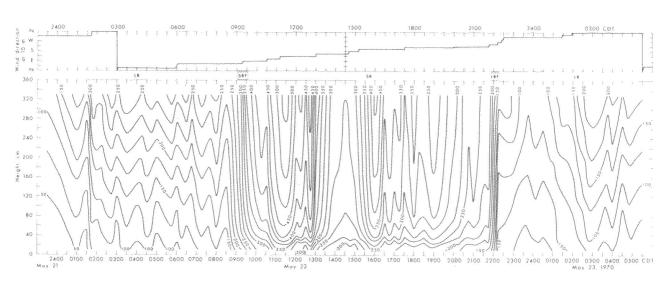


FIGURE 2.—Microstructure of the land breeze and sea breeze in the surface boundary layer on the beach face near Fort Walton Beach. LB stands for land breeze, SBF for sea-breeze front, SB for sea breeze, LBF for land-breeze front, and the numbers (such as 100, 150, 200, etc.) for U (cm/s).

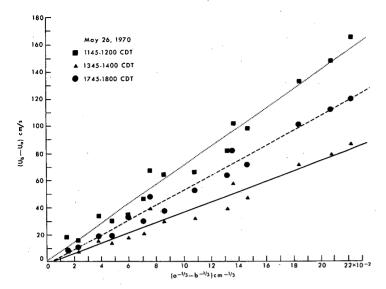


FIGURE 3.—Examples of the relationship between sea-breeze wind and elevation [(cf. eq (15a), (15b), (15c)] over the beach face near Fort Walton Beach.

Temperature and wind profiles in the atmospheric boundary layer below 100 m were based on measurements made from a meteorological tower at Eglin Air Force Base, Fla., which was about 10 km from the beach site. Measurements were made at four levels, approximately 2, 18, 54, and up to 100 m for the vertical temperature and at 4, 18, 54, and 100 m for the wind.

### Instrumentation

The main instrument used for this study was a portable Thornthwaite Wind Profile Register System (C. W. Thornthwaite Associates, Model 106)<sup>1</sup> with six-unit, three-cup, fast-response anemometers mounted 20, 40, 80, 160, 240, and 320 cm above the beach surface (fig. 1). The instrumentation and wind data reduction procedures have been described elsewhere (Hsu 1971a).

Temperatures were measured at 170, 360, and 550 cm above a grass-free berm surface by three identical recording hygrometry systems (Taylor Instrument Company, Series 76J, having readings within ± 1 percent of any given chart range). The sensors were mounted on a 10-m meteorological tower. An all-purpose wind-recording system (Science Associates Inc., No. 162) at the 10-m level above the surface made wind speed and direction measurements at the reference level.

Detailed information about the meteorological tower facility at Eglin AFB, along with related instrumentation and data processing procedures, will not be covered here because of military regulations.

## 4. STRUCTURE OF THE SEA BREEZE BELOW 10 m OVER THE BEACH SURFACE

Before we go into the studies of sea-breeze wind profile, some understanding of the microstructure and characteristics of this wind system may be helpful. The micro-

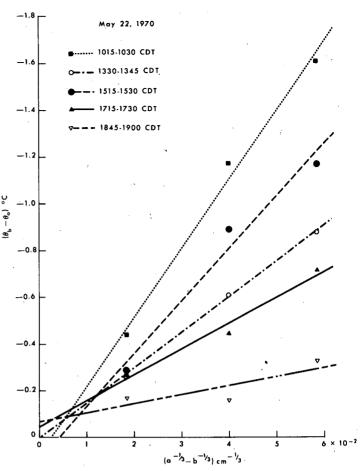


FIGURE 4.—Examples of the relationship between sea-breeze temperature and elevation [obtained from a set of equations parallel with eq (15a), (15b), (15c) for the temperature profiles as listed in table 2] over the grass-free berm surface near Fort Walton Beach.

structure of the sea breeze in the surface boundary layer should be composed of at least the following major characteristics. After the passage of the sea-breeze front in the morning, wind direction should shift clockwise in the Northern Hemisphere (Coriolis effect): that is, from a land breeze to a sea breeze, and the wind speed should increase. Meanwhile, cooler temperatures should prevail. Toward evening, the wind should become weaker because of the diminishing difference in air temperature between land and sea until the onset of the land-breeze front. This sequence is shown in figure 2. Some temperature characteristics associated with the sea-breeze front in the area of concern have been studied and presented elsewhere (Hsu 1969). Further evidence on the temperature profiles in the surface boundary layer is given later in table 2 (cf. fig. 4).

Since our immediate concern is to examine the validity of eq (11) and (12) under sea-breeze conditions, let us proceed as follows. First, eq (11) can be written as

$$U(z_2) - U(z_1) = 3 \left( \frac{U_*^{5\bar{\theta}}}{\lambda^2 q |\theta_*|} \right)^{1/3} (z_1^{-1/3} - z_2^{-1/3})$$
 (14)

<sup>&</sup>lt;sup>1</sup> Mention of a commercial product does not constitute endorsement.

Table 1.—Sea-breeze wind (cm/s) profiles in the surface boundary layer on the beach face near Fort Walton Beach, Fla., on May 22, 1970

Height Least-squares values 15-min ending Correla-20 cm 40 cm 80 cm 160 cm 240 cm 320 cm time (CDT) (cm/s) (cm/s) (cm/s) (cm/s) (cm/s) (cm/s) 0.61 25.1 . 69 21.8 . 66 19.7 . 73 15.6 0900\* .86 9.6 15† .98 2.6 30t .99 .96 45t 9.1 .99 . 99 5.1 . 99 4.1 79 .99 2.2 .99 -0.0 . 99 0.1 .99 -0.2 .99 2.4 . 99 0.1 .99 .99 .98 -1.4 .98 .98 -1.6 .98 -3.8 .97 -2.8 -1.9 -3.1 -1.3 .98 -2.3.99 . 99 -3.2.99 .99 -2.0.99 -1.5 .98 -2.8.99 -2.5.98 -4.2.98 .99 -2.9.98 -4.8.98 -4.3.99 -3.1 .99 -3.7-3.5.99 .99 -4.6.99 -3.3.98 -5.2.98 -4.2.98 -4.4.98 -4.2.98 -4.0.98 -4.2.98 -4.0.98 -3.7 .99 -1.0.92 6.8 21.9

or, between any two heights  $a(=z_1)$  and  $b(=z_2)$ , we have

$$U_b - U_a = 3 \left( \frac{U_*^{5\bar{\theta}}}{\lambda^2 g |\theta_*|} \right)^{1/3} (a^{-1/3} - b^{-1/3}). \tag{15a}$$

This may be written

$$y = a_0 + a_1 x \tag{15b}$$

Table 2.—Sea-breeze temperature (°C) profiles in the surface boundary layer on a grass-free berm surface near Fort Walton Beach, Fla., on May 22, 1970

| 15-min.     | Height |        |        | Least-squares values      |                                    |  |
|-------------|--------|--------|--------|---------------------------|------------------------------------|--|
| ending time | 170 cm | 360 cm | 550 cm | Correlation coefficient r | y axis intercept<br>a <sub>0</sub> |  |
| (CDT)       | (°c)   | (°c)   | (°c)   |                           | (°c)                               |  |
| 0900        | 27, 22 | 26.22  | 26.11  | 0.93                      | -0.25                              |  |
| 15          | 28.00  | 26.94  | 26.44  | 1.00                      | . 01                               |  |
| 30          | 27.61  | 26.83  | 25, 89 | 0.75                      | . 41                               |  |
| 45          | 27.28  | 26.50  | 25.83  | .91                       | . 22                               |  |
| 1000        | 27.28  | 26.44  | 25.72  | . 91                      | . 24                               |  |
| 15          | 27.22  | 26, 39 | 25.67  | .90                       | . 24                               |  |
| 30          | 27.50  | 26.33  | 25.89  | 1.00                      | 07                                 |  |
| 45          | 27.50  | 26.56  | 25.78  | 0.92                      | . 25                               |  |
| 1100        | 27.22  | 26.22  | 25.78  | 1.00                      | 02                                 |  |
| 15          | 26.94  | 26.17  | 25.72  | 0.99                      | . 07                               |  |
| 30          | 26.67  | 26.11  | 25.56  | . 85                      | . 21                               |  |
| 45          | 26.61  | 26.11  | 25.56  | . 80                      | . 23                               |  |
| 1200        | 26, 67 | 26.11  | 25.61  | . 89                      | .17                                |  |
| 15          | 26.67  | 26.11  | 25, 56 | . 85                      | . 21                               |  |
| 30          | 26.67  | 26.06  | 25.61  | .95                       | .12                                |  |
| 45          | 26,72  | 26.11  | 25.67  | .96                       | .11                                |  |
| 1300        | 26.89  | 26.17  | 25.72  | .98                       | . 08                               |  |
| 15          | 26.89  | 26, 28 | 25.83  | .95                       | .12                                |  |
| 30          | 26.94  | 26, 22 | 26,00  | .98                       | 08                                 |  |
| 45          | 26.94  | 26.33  | 26.06  | 1.00                      | 01                                 |  |
| 1400        | 27, 11 | 26, 56 | 26.11  | 0.92                      | .14                                |  |
| 15          | 27.11  | 26.61  | 26.11  | . 84                      | . 19                               |  |
| 30          | 26.94  | 26.61  | 26.11  | . 62                      | . 25                               |  |
| 45          | 27.00  | 26, 61 | 26.11  | .71                       | . 23                               |  |
| 1500        | 27.44  | 26.56  | 26.33  | .97                       | 13                                 |  |
| 15          | 27.67  | 26.67  | 26.61  | .91                       | 29                                 |  |
| 30          | 27.78  | 26.89  | 26.61  | .99                       | 09                                 |  |
| 45          | 27.44  | 26.78  | 26.17  | . 88                      | . 22                               |  |
| 1600        | 27.66  | 26.56  | 26.11  | . 97                      | . 10                               |  |
| 15          | 27.17  | 26.39  | 26.11  | .99                       | 06                                 |  |
| 30          | 27.22  | 26.50  | 26.22  | 1.00                      | 04                                 |  |
| 45          | 26.94  | 26.61  | 26.06  | 0.56                      | . 28                               |  |
| 1700        | 26.56  | 26.33  | 25.72  | . 33                      | . 36                               |  |
| 15          | 26.33  | 26.06  | 25.61  | . 56                      | . 23                               |  |
| 30          | 26.39  | 25.94  | 25.67  | .99                       | . 04                               |  |
| 45          | 26.39  | 26.06  | 25.67  | . 76                      | .17                                |  |
| 1800        | 26, 22 | 26.06  | 25.72  | . 43                      | . 19                               |  |
| 15          | 26.11  | 26.06  | 25.67  | .76                       | . 28                               |  |
| 30          | 26.11  | 25.94  | 25.61  | . 48                      | . 18                               |  |
| 45          | 26.06  | 25.89  | 25.56  | . 48                      | .18                                |  |
| 1900        | 25.83  | 25.67  | 25.50  | . 82                      | . 07                               |  |
| 15          | 25.67  | 25.61  | 25.44  | . 31                      | .10                                |  |
| 30          | 25.50  | 25.56  | 25.22  | 18                        | . 26                               |  |
| 45          | 25.39  | 25.50  | 25.17  | 28                        | . 27                               |  |
| 2000        | 25, 22 | 25.44  | 25.06  | 40                        | . 34                               |  |
| 15          | 25.06  | 25.28  | 25.00  | 48                        | . 27                               |  |
| 30          | 25.00  | 25.22  | 25.00  | 54                        | . 23                               |  |
| 45          | 25.00  | 25.11  | 25.00  | 54                        | .11                                |  |
| 2100        | 25.00  | 25.11  | 25.00  | 54                        | .11                                |  |
| 15          | 25.00  | 25.11  | 25.00  | 54                        | .11                                |  |
| 30          | 24.94  | 25.06  | 25.00  | 69                        | . 08                               |  |
| 45          | 24.89  | 25.06  | 25.00  | 74                        | .10                                |  |
| 2200        | 24.67  | 25.06  | 25.00  | 79                        | . 01                               |  |

where

and

$$y=U_{b}-U_{a},$$
 $a_{0}=0,$ 
 $a_{1}=3\left(\frac{U_{*}^{5\overline{\theta}}}{\lambda^{2}g|\theta_{*}|}\right)^{1/3},$ 
 $x=a^{-1/3}-b^{-1/3}.$ 
(15c)

We plot the observations for each run in the form y against x, plotting one point for each available pair of heights. Equation (15b) shows that, if the data do follow the free convection form, the points lie on a straight line. This method is similar to that used by Webb (1970).

<sup>\*</sup>For reference only: land-breeze regime

<sup>†</sup>For reference only: sea-breeze or land-breeze fronts

Table 3.—Sea-breeze temperature (°F) profiles at Eglin AFB, Fla., near Fort Walton Beach on May 21, 1969

| <b></b>                    | Height |       |               |        | Least-squares values         |                                       |
|----------------------------|--------|-------|---------------|--------|------------------------------|---------------------------------------|
| 15-min<br>ending -<br>time | 6 ft   | 54 ft | ght<br>162 ft | 300 ft | - Correlation<br>coefficient | y axis<br>intercept<br>a <sub>0</sub> |
|                            |        |       |               |        | ··                           |                                       |
| (CDT)                      | (°F)   | (°F)  | (°F)          | (°F)   |                              | (°F)                                  |
| 1000                       | 85.31  | 84.07 | 83.49         | 83, 15 | 0.97                         | 0.24                                  |
| 15                         | 87.19  | 85.11 | 84.05         | 84.06  | .98                          | . 05                                  |
| 30                         | 87.29  | 85.11 | 84.04         | 84.29  | .97                          | 12                                    |
| 45                         | 87.30  | 85.20 | 84.83         | 84.97  | .98                          | 37                                    |
| 1100                       | 88.18  | 85.58 | 84.87         | 85.16  | .98                          | 41                                    |
| 15                         | 87.32  | 85.76 | 85.03         | 84.79  | .99                          | .16                                   |
| 30                         | 88.64  | 86.58 | 85.72         | 85.57  | .99                          | . 07                                  |
| 45                         | 88.95  | 86.98 | 86.07         | 86.08  | .98                          | . 01                                  |
| 1200                       | 89.14  | 87.16 | 86.21         | 85.86  | .98                          | . 26                                  |
| 15                         | 90.11  | 87.81 | 86.58         | 86.44  | .98                          | . 19                                  |
| 30                         | 89.23  | 87.22 | 86.61         | 86.49  | 1.00                         | 06                                    |
| 45                         | 88.94  | 86.95 | 86.48         | 86.19  | 1.00                         | 01                                    |
| 1300                       | 90.52  | 88.38 | 87.35         | 86.85  | 0.98                         | .36                                   |
| 15                         | 91.42  | 88.72 | 87.47         | 87.45  | .98                          | .03                                   |
| 30                         | 91.44  | 88.36 | 87.50         | 87.66  | .99                          | 35                                    |
| 45                         | 91.71  | 88.82 | 87.97         | 88.04  | .99                          | 26                                    |
| 1400                       | 91.93  | 89.59 | 88.64         | 88.79  | .98                          | 15                                    |
| 15                         | 91.71  | 89.90 | 88.96         | 88.56  | .98                          | . 37                                  |
| 30                         | 91.83  | 89.37 | 88.60         | 88.45  | 1.00                         | 06                                    |
| 45                         | 91.68  | 89.14 | 88.58         | 88.49  | 0.99                         | 22                                    |
| 1500                       | 89.95  | 88.53 | 88, 20        | 87.51  | .93                          | . 31                                  |
| 15                         | 92.27  | 90.68 | 89,88         | 89.31  | .95                          | . 42                                  |
| 30                         | 90.01  | 88.83 | 88.45         | 87.81  | .91                          | . 35                                  |
| 45                         | 91.98  | 90.39 | 89.78         | 89.22  | .97                          | .32                                   |
| 1600                       | 91.73  | 89.28 | 88.67         | 88, 83 | .98                          | 19                                    |
| 15                         | 91.60  | 89.82 | 89.32         | 88.90  | .99                          | . 13                                  |
| 30                         | 91.04  | 89.47 | 89.10         | 88.74  | .99                          | .13                                   |
| 45                         | 90.37  | 89.36 | 89.01         | 88.26  | .99                          | .08                                   |
| 1700                       | 89.65  | 88.75 | 88.55         | 87.97  | .82                          | . 45                                  |
| 15                         | 89.57  | 88.66 | 88.50         | 87.94  | .86                          | . 29                                  |
| 30                         | 88.84  | 88.16 | 88.10         | 87.47  | .87                          | . 25                                  |
| 45                         | 88.12  | 87.61 | 87.58         | 87.00  | .70                          | .30                                   |
| 1800                       | 87.06  | 86.74 | 86.81         | 86.32  | .37                          | . 22                                  |

Equations (15b) and (15c) have also been obtained by the least-squares technique. This method of data analysis and the results are illustrated in figure 3. Tables 1 and 4 give the least-squares values of each correlation coefficient, r, as well as the y-axis intercept,  $a_0$ .

Similar analyses were made for temperature profiles under sea-breeze conditions whenever wind profiles were measured. Examples are given in figure 4 and tables 2 and 3.

Figure 5 shows some of the measured sea-breeze wind profiles. Note that, for brevity, only those profiles that do not overlap are plotted in the figure. For the entire diurnal variation of the profile, however, table 1 should be consulted. Also included in figure 5 is an example of the predicted sea-breeze wind profile using eq (13) and those parameters listed in the figure. The choice of the value of  $\lambda \approx 1$  is based on the findings by Priestley (1959), Deardorff and Willis (1967), and Dyer (1967).

The shape of the predicted sea-breeze wind profile is in excellent agreement with those observed (fig. 5). In fact, table 1 gives considerable evidence that, in the whole sea-breeze range from 1000 to 2200 cpt, the least-squares values of each correlation coefficient, r, is greater than 0.96 and that -5.2 cm/s $< a_0 < 5.2$  cm/s, which is within the experimental error. Examples of the sea-breeze temperature profiles are listed in table 2. Because temperatures were measured at only three levels, the correlation coefficients for these profiles were naturally less than those for the wind profiles. Nevertheless, in the major sea-

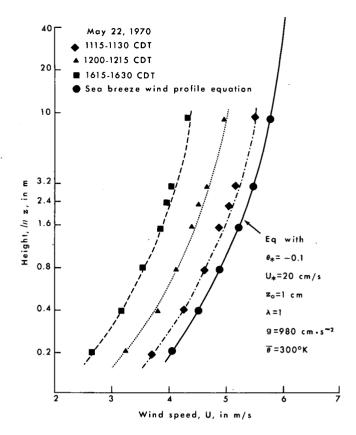


FIGURE 5.—Examples of measured sea-breeze wind profiles in the surface boundary layer near Fort Walton Beach. Included also is the predicted sea-breeze wind profile equation with parameters from eq (13) specified in the figure.

Table 4.—Sea-breeze wind (kt) profiles at Eglin AFB, Fla., near Fort Walton Beach on May 21, 1969

| 15-min<br>ending –<br>time | Height       |                         |                |                       | Least-squares values      |                                       |
|----------------------------|--------------|-------------------------|----------------|-----------------------|---------------------------|---------------------------------------|
|                            | 12 ft        | 54 ft                   | 162 ft         | 300 ft                | - Correlation coefficient | y axis<br>intercept<br>a <sub>0</sub> |
| (CDT)                      | (kt)         | (kt)                    | (kt)           | (kt)                  | <del></del>               | (kt)                                  |
| 1000                       | 4.79         | 5.15                    | 5. 24          | 6.31                  | 0. 21                     | 0.59                                  |
| 15                         | 7.90         | 9.45                    | 8.99           | 8.60                  | .70                       | 81                                    |
| 30                         | 6.28         | 7.35                    | 7.91           | 8.48                  | .95                       | . 24                                  |
| 45                         | 6.63         | 8, 28                   | 8.88           | 9.13                  | .99                       | 10                                    |
| 1100                       | 7.88         | 9.03                    | 9.55           | 9.13<br>9. <b>5</b> 9 | .99                       | 10<br>12                              |
| 15                         | 4.19         | 4.90                    | 6.58           | 7.23                  | . 69                      | 12<br>.74                             |
| 30                         | 6.68         | 4.90<br>8.39            | 8.68           | 7. 23<br>8. 56        | .93                       | 48                                    |
| 45                         | 6.80         | 8.29                    | - 8.83         | 10.23                 | .93<br>.78                | 48<br>.63                             |
| 1200                       | 5.76         | 6.52                    | - 6.83<br>7.57 | 8. 61                 | . 66                      | . 77                                  |
| 1200                       | 7.32         | 8.80                    | 9.50           | 9.76                  | 1.00                      | 02                                    |
| 30                         | 8.47         | 10.48                   | 10.77          | 11.04                 | 0.95                      | 02<br>29                              |
| 45                         | 6.67         | 7.75                    | 8.48           | 9.46                  | .82                       | 54                                    |
| 1300                       | 7.83         | 9.32                    | 9.25           | 9.40                  | .88                       | 34                                    |
| 1500                       | 8, 59        | 9. <b>3</b> 2<br>10. 60 | 9, 20          | 9.39                  | .98                       | 34<br>27                              |
| 30                         | 8.09<br>7.91 | 8.82                    | 9.32           | 9.14                  | .94                       | 27<br>20                              |
| 45                         |              | -                       |                |                       |                           | 20<br>29                              |
| 1400                       | 8.61<br>7.83 | 9.96<br>9. <b>3</b> 5   | 10.34<br>10.30 | 10.26                 | . 96<br>. 99              | 29<br>. 07                            |
|                            |              |                         |                | 10.59                 |                           | . 11                                  |
| 15<br>30                   | 6.75         | 7.86                    | 8.35           | 8.76                  | :99                       | . 65                                  |
|                            | 5.42         | 6.39                    | 6.64           | 8.00                  | . 56<br>. 99              | . 14                                  |
| 45                         | 8.30         | 9.75                    | 10.53          | 10.99                 |                           | 19                                    |
| 1500                       | 7.49         | 9.13                    | 9.50           | 9.78                  | .97                       | .03                                   |
| 15                         | 8.05         | 9.28                    | 9.74           | 10.09                 | . 99                      | . 03<br>34                            |
| 30                         | 8.20         | 10.11                   | 11.14          | 10.98                 | .97                       | 08                                    |
| 45                         | 9.29         | 11.46                   | 12.23          | 12.66                 | 1,00<br>0,99              | 09                                    |
| 1600                       | 8.37         | 10.07                   | 10.57          | 10.91                 | . 87                      | 09<br>74                              |
| 15                         | 11.45        | 13.86                   | 13.80          | 13.70                 |                           | 74<br>27                              |
| 30                         | 9.06         | 11.35                   | 12.23          | 12.35                 | .99                       | 27<br>02                              |
| 45                         | 9.90         | 12.39                   | 13.19          | 13.91                 | .99                       | 02<br>08                              |
| 1700                       | 8.50         | 10.51                   | 10.76          | 11.42                 | .94                       | 05                                    |
| 15                         | 9.11         | 11.28                   | 12.44          | 12.88                 | 1.00                      | 05<br>. 21                            |
| 30                         | 7.36         | 9.24                    | 10.08          | 10.82                 | 0.98                      | . 32                                  |
| 45                         | 6.64         | 8. 26                   | 8.63           | 9.68                  | . 88                      |                                       |
| 1800                       | 5.81         | 6.98                    | 8.54           | 9.71                  | .76                       | .90                                   |

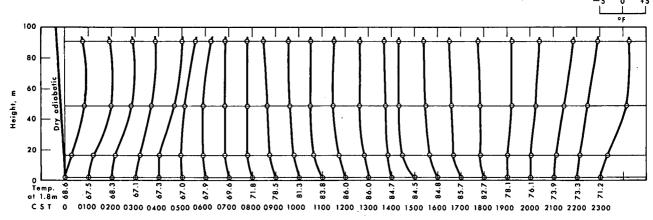


FIGURE 6.—Diurnal variation of temperature between 1.8 and 90.9 m at Eglin AFB, near Fort Walton Beach, May 20, 1969.

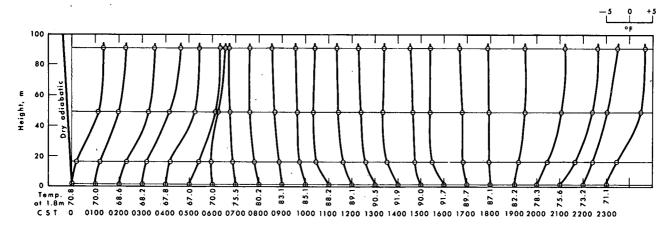


FIGURE 7.—Same as figure 6 for May 21, 1969.

breeze regime from 0900 to 1900 cpt, we obtained values for r that are highly significant and values for  $a_0$  that are within the acceptable experimental error. In other words, these observations verify that the sea breeze is in the atmospheric free convection regime and that its wind and temperature profiles in the surface boundary layer can be represented by eq (11) and (12), respectively.

# 5. SEA-BREEZE TEMPERATURE AND WIND PROFILES BELOW 100 m ON AN INLAND SITE

To further support the results given in section 4, we present independent measurements of sea-breeze temperature and wind profiles below 100 m on an inland site. As mentioned previously, these profiles are based on measurements made from a meteorological tower at Eglin AFB, near Fort Walton Beach. Because land and sea breezes, as well as their fronts near the surface, were observed on May 20 and 21, 1969 (Hsu 1969), these 2 days were selected for this study.

Figures 6 and 7 show the hourly variation of the temperature profile between 1.8 and 90.9 m for May 20 and 21, respectively. For reference, times of sunrise and sunset for these 2 days were approximately 0504 and 1849 csr, respectively. Since the lapse rate,  $\gamma$ , of the actual temperature, T, is defined as the rate of T decrease with height, z, (i.e.,  $\gamma = -dT/dz$ ) and since the dry adiabatic lapse rate,  $\gamma_d$ , is 0.98°C/100 m (or 5.4°F/1,000 ft), the

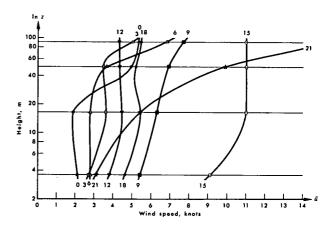


FIGURE 8.—Wind profiles between 3.6 and 90.9 m at Eglin AFB May 20, 1969.

stability criteria for the unsaturated air may be written as (e.g., Haltiner and Martin 1957)

$$\gamma{>}\gamma_d$$
 unstable,  $\gamma{=}\gamma_d$  neutral, and  $\gamma{<}\gamma_d$  stable.

Comparing the hourly temperature profiles with the dry adiabatic lapse rate shown on the left of figures 6 and 7, we see that, in general, conditions are stable at night and

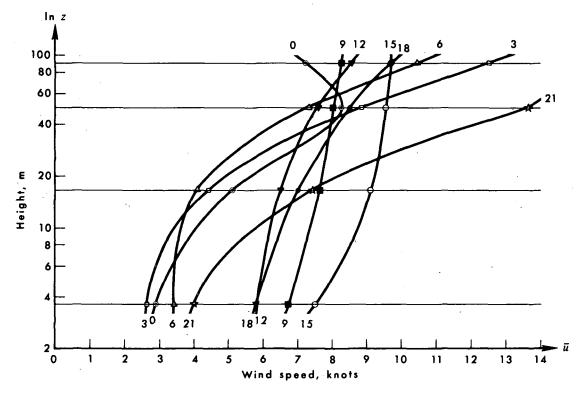


FIGURE 9.—Same as figure 8 for May 21, 1969.

unstable during the day over the coastal zone. Sea-breeze temperature profiles in the atmospheric boundary layer, which is also in the free convection regime, are given in table 3.

From Figures 6 and 7, the following features are also noted (cf. Sutton 1953, pp. 190-192):

- 1. During the day, temperature decreases with height, rapidly in the lowest layers and more slowly at greater heights. Furthermore, the cooling effect of the sea breeze tends to modify the profile to a near-isothermal one, even though the lowest layers may still be in the superadiabatic lapse rate situation because of the surface condition (cf. Hsu 1969).
- 2. At night, temperature increases with height (i.e., the inversion case) with the greatest gradient in the middle layers instead of in the lowest layers. In other words, a pool of cold air forms in the lowest layers during the night. The cool pool phenomenon associated with land-breeze genesis on the coast has been studied in more detail by Hsu (1970b).

According to Sutton (1953, p. 230), the normal diurnal variation of the coastal wind tends to be masked by land breezes and sea breezes. The diurnal variations of wind speed between 3.6 and 90.9 m for May 20 and 21 under the land- and sea-breeze conditions are shown in figures 8 and 9, respectively. Note that the wind profiles are plotted on semilogarithmic paper so that a straight line may be fitted for the neutral stability; that is, for the law of logarithmic wind profile (e.g., Haltiner and Martin 1957). For the sake of clarity, profiles are plotted for every 3 hr instead of for each hour.

Figures 8 and 9 clearly show that the wind profile is concave either upward or downward except around midmorning (0900 LST) when the transitional period occurs between land breeze and sea breeze. (See figs. 1 and 2 of Hsu 1969.) Caution should be used, therefore, in applying

the law of logarithmic wind profile in the coastal zone, at least under land- and sea-breeze conditions. Furthermore, particular attention should be given to the afternoon seabreeze wind profile (1500 cst) in figures 8 and 9. Excellent agreement can be seen between the shapes of these profiles with that predicted by eq (13), as shown in figure 5, particularly around 1500 cst on May 21, 1969 (fig. 9). Further description of the sea-breeze wind profile in the atmospheric boundary layer is given in table 4. The typical nighttime land-breeze profile (2100 cst) is also shown in figures 8 and 9.

## 6. CONCLUDING REMARKS

Expressions for the wind and temperature profiles [eq (11) and (12)] are derived for the sea-breeze regime in the surface boundary layer, assuming that free convection conditions exist. A case study of the free convection regime is made to determine the validity of these equations. The results of this study verify that the sea breeze is in the atmospheric free convection regime and that its wind and temperature profiles in the surface boundary layer can be represented by the equations.

Murray (1972) has shown that the sea breeze is effective in generating waves and currents, which in turn transport sediments in the littoral environment. Eolian sand transport (Inman et al. 1966, Hsu 1971b) and air pollution (Neiburger 1969) in the coastal zone are also closely controlled by this localized wind system. We recommend, therefore, that similar experiments be conducted for both sea- and land-breeze conditions in other geographical regions (Defant 1951, Baralt and Brown 1965) using more detailed measurements such as those of Wyngaard et al. (1971) and Hembree (1971).

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